conditions and indicates that the mechanism of thermoacoustic oscillations for surface boiling (P <  $P_{cr}$ ) and that for pseudoboiling (P >  $P_{cr}$ ) are the same.

### NOTATION

V, volume of the pseudobubbles; P, pressure;  $P_{cr}$ , critical pressure;  $t_{cr}$ , critical temperature;  $t_{in}$ ,  $t_{out}$ , temperatures of the n-heptane at the input to the working section and at the output from it;  $t_s$ , temperature of the cooled surface of the heat-dissipating element; q, heat flow;  $W_{\gamma}$ , mass velocity.

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THEORY OF THE TEMPERATURE STABILIZATION PROCESS IN GAS-CONTROLLED HEAT PIPES

L. L. Vasil'ev and S. V. Konev

UDC 536.248.2

This paper presents results of an analytical investigation of the temperature-stabilization process in gas-controlled heat pipes. Expressions are obtained for the temperature-sensitivity coefficients.

Heat-pipe technology includes the use of heterogeneous heat-transmitting systems with constant-volume change of state, i.e., gas-controlled heat pipes, which possess the tempera-ture-stabilization property.

The investigators in [1] encountered phenomena associated with blockage of the condenser by a noncondensible gas. Cotter [3] noted that the length of the blocked zone depends on the heat flux. Katzoff [2] suggested using the condenser blockage effect for temperature stabilization. Bienert [4] was the first to describe analytically the temperature-stabilization process using a gas-controlled heat pipe, which was later accomplished by Marcus [5]. More complete information on gas-controlled heat pipes can be found in [6].

The present paper deals with an analytical investigation of the gas-controlled heat pipe and pays particular attention to the temperature-sensitivity coefficient.

In examining the temperature-stabilization process employing a gas-controlled heat pipe, we use the model shown in Fig. 1. In analyzing this one-dimensional model we make the following assumptions: 1) The heat pipe is a closed thermodynamic system; 2) the vapor-gas mixture in the blocked zone obeys all the ideal gas laws; 3) the vapor and the gas are incompressible; 4) the vapor motion is laminar; 5) the heat pipe is horizontal; 6) the heatpipe regime is evaporative.

## Equation of State for the Vapor-Gas in a Gas-Controlled

### Heat Pipe

In the equilibrium state of a gas-controlled heat pipe, in the absence of energy exchange with the surrounding medium, and with assumption 1, the heat-transfer agent and the

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Fig. 1. Model of a gas-controlled heat pipe.

noncondensible gas are subject to the following conditions:

$$m_{\rm hta} = m_{\rm y} + m_{\rm f} = {\rm const},\tag{1}$$

$$V_{\mathbf{v},\mathbf{g},\mathbf{l}} = V_{\mathbf{v},\mathbf{g}} + V_{\mathbf{l}} = \text{const},$$
(2)

$$P_{\mathbf{v},\mathbf{g}} = P_{\mathbf{v}} + P_{\mathbf{g}}.$$
 (3)

We obtain the vapor pressure on the saturation line from the widely known Clausius-Clapeyron equation:

$$P_{\mathbf{v}} = \exp\left(C - \frac{M_{\mathbf{v}}r^*}{R_0T}\right). \tag{4}$$

In Eq. (4) the constant of integration has a particular value for each heat-transfer agent, and the values of C calculated here are given in Table 1.

In the nonequilibrium state the thermal conditions will vary in a gas-controlled heat pipe. If the range of vapor temperature change is small, i.e., we are concerned with a gascontrolled heat pipe having a supplementary volume, we can use the Clausius-Clapeyron equation in the form

$$\ln \frac{P_2}{P_1} = \frac{M_{\rm V}r^*}{R_0} \left[ \frac{T_2 - T_1}{T_1 T_2} \right]$$
 (5)

As is known [7], the temperature-stabilization process begins to operate from a specific value of the transmitted heat flux, called the minimum value. Therefore, after the binary vapor-gas mixture is separated, the equation for the total barometric pressure in a gascontrolled heat pipe will have the form

$$P = P_{a} = P_{b}.$$
 (6)

In the blocked zone the molecules of gas and vapor have the same temperature, and therefore the Dalton law will hold. Taking account of the equation of state of an ideal gas and of the Clausius-Clapeyron equation for the vapor, both in the active and blocked zones, we obtain a general expression for the state of the vapor-gas mixture in a gas-controlled heat pipe, operating under steady-state conditions:

$$\frac{R_0 T_g}{V_b} \frac{m_g}{M_g} = \exp\left(C - \frac{M_v r^*}{R_0 T_{v,a}}\right) - \exp\left(C - \frac{M_v r^*}{R_0 T_{v,b}}\right).$$
(7)

Neglecting the partial pressure of the vapor in the blocked zone, we can represent its volume in the form

$$V_{\mathbf{b}} = \frac{m_{\mathbf{g}}R_{\mathbf{0}}T_{\mathbf{g},\mathbf{b}}}{M_{\mathbf{g}}} \left[ \exp\left(C - \frac{M_{\mathbf{v}}r^{*}}{R_{\mathbf{0}}T_{\mathbf{v},\mathbf{a}}}\right) \right]^{-1}.$$
(8)

Heat-transfer agent	Chemical formula	М	т <sub>с</sub> , °К	$\frac{r^*M}{R_s}$ , K	$\frac{\sigma \rho r}{\mu} 10^{-4}$ . W/cm <sup>2</sup>	C for P, torr
agent Helium Hydrogen Neon Nitrogen Carbon monoxide Fluorine Argon Oxygen Methane Krypton F-14 Xenon Ethylene Ethane Acetylene F-23 F-13 F-16 Propylene Propane F-22 F-115 Ammonia F-12 F-40 Isobutane F-14 F-14 F-114 F-21 F-11 Diethyl ether Pentane F-113 Methanol Carbon tetrachloride Ethyla cetate Ethanol Benzene Acetone Propanol Heptane Water Toluene Pyridine	He He Hs Ne No CC Far O CH T C C H C C H C C H C C H C C H C C H C C H C C H C C H C C H C C H C C H H S C C C A H C C H T C C C A H C C C H T C C C C A H C C C C C A H C C C C C C C	4.00 2.01 20,18 28,01 28,00 38,00 39,94 32.00 16,00 83,800 131,3 28,05 30,00 26,03 70.00 104,5 138,00 42,07 44,09 86,48 154,0 17,00 120,9 50,49 58,12 100,4 171,0 102,9 137,4 74,10 72,15 187,4 32,00 153,8 88,10 46,07 78,11 58,08 60,09 100,2 18,02 92,13 79,00	4.21 20,38 27,09 77,36 81,61 84,95 87,29 90,18 111,7 119,7 145,2 165,1 169,1 184,5 189,6 191,2 191,8 194,9 225,5 231,1 234,4 234,5 239,8 243,4 249,4 261,4 264,2 276,7 282,1 301,9 307,6 309,2 320,7 3351,5 353,3 359,3 370,4 371,7 373,2 383,7 389,3 390,0	R, 4424 11.4 116 213 685 722 774 770 841 1002 1112 1553 1549 1516 1803 2095 2056 1906 1983 2280 2384 2384 2452 2668 2600 2716 3061 2908 3133 3139 3408 4424 3639 3408 4424 3639 3408 4424 3639 3408 3427 5266 3801 3726 3190 3915 5894 3487 4347 4347 4347 4347 4347 4347 5274	W/cm²           %/cm²           838           518           3986           8279           9442           17981           9666           17205           19199           962           2872           16576           23054           31941           23425           13569           8916           5990           11776           10113           12528           3150           20419           9675           29415           14921           9534           5292           15658           11333           17544           9990           49175           11990           19482           26676           42710           30237           16354           12857           48955           17515           61921	torr 9,363 12,347 14,517 15,509 15,766 15,476 15,981 16,625 15,945 17,350 16,037 15,620 16,427 17,704 17,406 16,592 16,834 16,766 16,633 14,543 16,821 18,590 16,729 17,352 16,601 16,935 17,355 17,355 16,840 16,840 16,805 17,281 19,755 17,281 19,755 17,055 17,281 19,755 17,281 19,755 17,055 17,281 19,755 17,055 17,281 19,755 17,281 19,755 17,025 17,187 22,448 15,743 17,821 19,640 17,187 15,267 17,187 15,267 17,187 15,267 17,187 15,267 17,187 12,2448 15,743 17,821 10,492 17,187 15,267 16,492 17,187 15,267 17,187 15,267 17,187 15,267 17,187 15,267 15,267 17,187 15,267 17,187 15,267 17,187 15,267 17,187 15,267 17,187 15,267 17,187 15,267 17,187 15,267 17,187 15,267 17,187 15,267 17,187 17,187 15,267 17,187 15,267 17,187 15,267 17,187 17,187 17,187 17,187 15,267 17,187 17,187 17,187 17,187 15,267 17,187 15,267 17,187 15,267 17,187
Chlorobenzene o-Xylene Cumene Naphthalene Diphenyl Dowtherm Diphenyl ether Glycerol	$\begin{bmatrix} C_{8}H_{5}CI \\ C_{8}H_{10} \\ C_{9}H_{12} \\ C_{10}H_{8} \\ C_{12}H_{10} \\ \hline \\ C_{12}H_{10} \\ \hline \\ C_{3}H_{5}(OH)_{3} \end{bmatrix}$	112.6 106.2 120.2 128.2 154.2 165.8 170.1 92.04	405,2 417,6 425,6 491,0 528,2 530,1 531,0 563,0	4497 4501 4682 4963 5970 5850 5769 8749	21874 20333 13057 — — — —	20,402 17,753 17,433 17,672 16,763 17,957 17,690 17,519 22,195

TABLE 1. Basic Parameters of Heat-Transfer Agents Used in Gas-Controlled Heat Pipes

For a linear gas-controlled heat pipe we can write expressions for the lengths of the blocked and the active zones:

$$L_{\rm b} = \frac{m_{\rm g} R_{\rm 0} T_{\rm g,b}}{M_{\rm g} F_{\rm g}} \left[ \exp\left(C - \frac{M_{\rm v} r^*}{R_{\rm 0} T_{\rm v,a}}\right) \right]^{-1},$$
(9)

$$L_{\mathbf{a}} = L_{\mathbf{c}} - \frac{m_{\mathbf{g}}R_{0}T_{\mathbf{g},\mathbf{b}}}{M_{\mathbf{g}}F_{\mathbf{g}}} \left[ \exp\left(C - \frac{M_{\mathbf{v}}r^{*}}{R_{0}T_{\mathbf{v},\mathbf{a}}}\right) \right]^{-1}.$$
 (10)

To obtain a high degree of temperature stabilization, an additional reservoir is used with a gas or an expanded volume. For gas-controlled heat pipes of this construction the expression (10) takes the form

$$L_{\mathbf{a}} = L_{\mathbf{c}} - \frac{m_{\mathbf{g}} R_0 T_{\mathbf{g},\mathbf{b}}}{M_{\mathbf{g}} F_{\mathbf{g}}} \left[ \exp\left(C - \frac{M_{\mathbf{v}} r^*}{R_0 T_{\mathbf{v}}}\right) \right]^{-1} + \frac{V_{\mathbf{r}}}{F_{\mathbf{v}}}.$$
 (11)



Fig. 2. Calculated vapor temperature as a function of transmitted heat flux. T<sub>v</sub>, °K; Q, W.

## Heat Transfer in a Gas-Controlled Heat Pipe

The thermal resistance of a simple (uncontrolled) heat pipe has the form

$$R_{\rm h,p} = R_{\rm e} + R_{\rm c} = \frac{R_{\rm e}'}{F_{\rm e}} + \frac{R_{\rm c}'}{F_{\rm c}}, \qquad (12)$$

where R is the thermal resistance referred to the heat removal or supply area and characterizes the heat pipe with the condition  $F_e \neq F_c$ . For a gas-controlled heat pipe Eq. (12) takes the form

$$R_{\rm gchp} = R_{\rm e} + \frac{R_{\rm a}R_{\rm b}}{R_{\rm a} + R_{\rm b}}.$$
(13)

Under the assumption of a constant cross section for the vapor flux along the condenser length, from Eqs. (10), (12), and (13) one can obtain the basic equation for heat transfer in a gascontrolled heat pipe:

$$Q = (T_{\rm v} - T_{\rm s}) \left\{ \frac{F_{\rm c}}{R_{\rm a}'} - \frac{R_{\rm b}' - R_{\rm a}'}{R_{\rm a}' R_{\rm b}'} \cdot \frac{\Pi m_{\rm g} R_0 T_{\rm g}}{F_{\rm v} M_{\rm g}} \left[ \exp\left(C - \frac{M_{\rm v} r^*}{R_0 T_{\rm v}}\right) \right]^{-1} \right\}.$$
 (14)

In engineering calculations of gas-controlled heat pipes we neglect the heat transfer through the blocked zone in many cases  $(R_b \rightarrow \infty)$ :

$$Q = \frac{\Pi (T_{\rm V} - T_{\rm s})}{R_{\rm a}'} \left\{ L_{\rm c} - \frac{m_{\rm g} R_{\rm o} T_{\rm b}}{F_{\rm v} M_{\rm g}} \left[ \exp \left( C - \frac{M_{\rm v} r^*}{R_{\rm o} T_{\rm v}} \right) \right]^{-1} \right\}.$$
(15)

The use of a supplementary reservoir or an elongated volume permits a high degree of temperature stabilization. For these structures and boundary conditions of the second and third kinds at the outer surface of the evaporator (a boundary condition of the third kind is assumed at the outer surface of the condenser), Eq. (15) takes the form

$$Q = \frac{\Pi (T_{\mathbf{v}} - T_{\mathbf{s}})}{R_{\mathbf{a}}'} \left\{ L_{\mathbf{c}} - \frac{V_{\mathbf{r}}}{F_{\mathbf{v}}} - \frac{m_{\mathbf{g}}R_{\mathbf{0}}T_{\mathbf{g}}}{M_{\mathbf{v}}F_{\mathbf{v}}} \left[ \exp\left(C - \frac{M_{\mathbf{v}}r^{*}}{R_{\mathbf{0}}T_{\mathbf{v}}}\right) \right]^{-1} \right\},$$
(16)

$$T_{\rm v} = T_{\rm s} + (T_{\rm true} - T_{\rm s}) \left\{ 2 + \frac{V_{\rm r}}{V_{\rm c}} - \frac{m_{\rm g} R_0 T_{\rm g}}{M_{\rm v} V_{\rm c}} \left[ \exp\left(C - \frac{M_{\rm v} r^*}{R_0 T_{\rm v,a}}\right) \right]^{-1} \right\}.$$
 (17)

Expression (17) was obtained from Eq. (15) under the assumption  $R'_e = R'_a$  and  $n_{h,p} = 1$ .

By way of example we calculated a gas-controlled heat pipe with the following parameters:  $L_c = 1 m$ ,  $d_v = 10^{-2} m$ ,  $R'_a = 10^{-1} m \cdot K/W$ , and  $T_s = 293^{\circ}K$ , the heat-transfer agent being methanol and the noncondensible gas being argon. The results are shown in Fig. 2, in the form of the relationship  $T_v = f(Q)$ . It was assumed in the calculations that  $Q_{min} = 0$ . One can see from the figure that the vapor temperature stabilization is greater, the higher the vapor temperature, or, in other words, the greater the mass of noncondensible gas, for constant geometrical parameters. The curves  $T_v = f(Q)$  for a gas-controlled heat pipe without an additional gas reservoir draw near to the curve  $T_v = f(Q)$  for a simple uncontrolled heat pipe



Fig. 3. The vapor temperature increment as a function of the ratio  $V_c/V_r$  (a) and of the absolute stabilization temperature (b).

as the transmitted heat flux increases. The slight slope of the curves near zero shows that a higher degree of temperature stabilization is achieved for small transmitted heat flux, corresponding to minimum vapor temperature in the stabilization range  $Q > Q_{min}$ . When an additional gas reservoir is used the slope of the curves  $T_v = f(Q)$  decreases; i.e., there is more vapor temperature stabilization for such heat pipes. Analysis of the curves shown in Fig. 2 indicates that a gas-controlled heat pipe with an additional gas reservoir can be regarded as a simple gas-controlled heat pipe in which the condenser length is increased by the amount  $V_r/F_v$ . Here the shorter the length of the active zone (for constant condenser length), the greater the degree to which the vapor temperature is maintained constant.

In developing gas-controlled heat pipes one must determine the volume of the supplementary reservoir to achieve minimum vapor temperature variation for maximum variation of transmitted heat flux. Using the fact that the number of moles of gas  $m_g/M_g$  is constant and also the conditions  $Q_{min} = 0$  and  $Q_{max} = (F_c/F_{sup})(T_{v.max} - T_s)$ , one can use Eq. (16) to obtain an expression for the ratio of the supplementary reservoir volume to the condenser volume:

$$\frac{V_{\mathbf{r}}}{V_{\mathbf{c}}} = \left[\frac{P_{\mathbf{v}\cdot\mathrm{max}}}{P_{\mathbf{v}\cdot\mathrm{min}}} - 1\right]^{-1}$$
(18)

Using Eq. (5), we obtain an expression for the ratio (18) in the following form:

$$\frac{V_{\mathbf{r}}}{V_{\mathbf{c}}} = \left[ \exp \frac{r^* M}{R_0} \left( \frac{T_{\mathbf{v} \cdot \text{max}} - T_{\mathbf{v} \cdot \text{min}}}{T_{\mathbf{v} \cdot \text{max}} \cdot T_{\mathbf{v} \cdot \text{min}}} \right) - 1 \right]^{-1}.$$
(19)

With the equations obtained one can calculate the volume of a gas-controlled reservoir for a given condenser volume as a function of the vapor pressure increment [Eq. (18)] or of the allowable vapor temperature increment [Eq. (19)].

# Temperature Sensitivity of a Gas-Controlled Heat Pipe

In the most general case the sensitivity coefficient is the ratio of an increment in the destabilizing parameter to an increment in the stabilized quantity. Analysis of the use of this parameter to evaluate the operation of heat pipes shows that in practice one can use both thermal or temperature coefficients and sensitivity coefficients relating to heat-flux density or gas pressure, and so on.



Fig. 4. Temperature-sensitivity coefficient for the external wall of the evaporator as a function of the vapor temperature-sensitivity coefficient  $\sigma_{e}^{\star}$ , W/°K.

For the parameter describing control of vapor temperature in a gas-controlled heat pipe, we use the temperature-sensitivity coefficient  $\sigma_v^* = dQ/dT_v$ . Sometimes one uses the thermalcontrol coefficient as a characteristic of a gas-controlled heat pipe, this being the inverse of the temperature-sensitivity coefficient. From the engineering viewpoint, one is most interested in the temperature-sensitivity coefficient at the surface of the evaporator  $\sigma_e^* = dQ/dT_e$  or of the condenser  $\sigma_c^* = dQ/dT_c$ . Without an appreciable error one can regard the characteristics as being linear for the majority of gas-controlled heat pipes with an additional gas reservoir, assuming that the heat transmission is constant along the heat pipe. Then from the practical viewpoint one is most interested in the temperature-sensitivity coefficient in the form

$$\sigma^* = \frac{Q_{\max} - Q_{\min}}{T_{\max} - T_{\min}} \,. \tag{20}$$

Analysis of this expression shows that  $\sigma^*$  may increase due to a decrease in  $Q_{\min}$  or to a decrease in the denominator. The temperature difference  $T_{\max} - T_{\min}$  can be expressed in terms of the volume ratio  $V_r/V_c$  [Eq. (19)]. To do this we write the exponent function in Eq. (19) in the form of a MacLaurin series:

$$\exp\left(\frac{r^*M}{R_0}\cdot\frac{T_{\mathbf{v},\max}-T_{\mathbf{v},\min}}{T_{\mathbf{v},\max}\cdot T_{\mathbf{v},\min}}\right) = 1 + \frac{r^*M}{R_0}\cdot\frac{(T_{\mathbf{v},\max}-T_{\mathbf{v},\min})}{T_{\mathbf{v},\max}\cdot T_{\mathbf{v},\min}} + \left(\frac{r^*M}{R_0}\cdot\frac{T_{\mathbf{v},\max}-T_{\mathbf{v},\min}}{T_{\mathbf{v},\max}\cdot T_{\mathbf{v},\min}}\right)^2 + \dots$$
(21)

In analyzing this expression we restrict attention to the first two terms, because the subsequent terms are small. Then, taking account of expressions (19) and (21), we can write the denominator in Eq. (20) in the following form:

 $\Delta T_{\mathbf{v}} = \frac{R_0 \overline{T}_{\mathbf{v}}^2}{Mr^*} \cdot \frac{V_{\mathbf{c}}}{V_{\mathbf{r}}}, \qquad (22)$ 

where the average vapor temperature is

$$\overline{T}_{\mathbf{v}}^2 = T_{\mathbf{v}.\max} \cdot T_{\mathbf{v}.\min} + \frac{\Delta T_{\mathbf{v}}^2}{4}$$

From Eq. (22) we can conclude that the vapor temperature increment increases with increase in the ratio  $V_c/V_r$ . Figure 3a shows a group of straight lines for some heat-transfer agents, calculated using Eq. (22). From the figure it can be seen that cryogenic heat-transfer agents possess appreciable advantages in comparison with low-temperature agents, since they have low vapor temperature increments  $\Delta T_v$ , which result from the low value of the stabilization temperature  $T_v$ .

To investigate the behavior of the function  $\Delta T_v = f(T)$  over the whole operating temperature range  $\Delta T_o = T_{cr} - T_{tr}$ ,  $\Delta T_v$  was calculated for methanol and nitrogen (Fig. 3b) heat pipes.

From analysis of Fig. 3b one can conclude that a gas-controlled heat pipe with a constant gas reservoir will show better thermal stabilization at temperatures close to the triple point.

Taking account of Eq. (22), one can write an expression for the general temperaturesensitivity coefficient with respect to the vapor:

$$\sigma_{\mathbf{v}}^{*} = \frac{\Pi L_{\mathbf{a} \cdot \max}}{R_{\mathbf{a}}^{\prime}} \cdot \frac{T_{\mathbf{v}} - T_{\mathbf{s}}}{\overline{T}_{\mathbf{v}}^{2}} \frac{Mr^{*}}{R_{0}} \cdot \frac{V_{\mathbf{r}}}{V_{\mathbf{c}}}$$
(23)

The expression obtained for the temperature-sensitivity coefficient is valid for small changes in vapor temperature. It follows from Eq. (23) that to obtain large values of  $\sigma_{\rm V}^{\rm v}$  one must choose a heat-transfer agent with a greater curvature in the relationship between vapor pressure and temperature at the saturation line. A promising method for increasing  $\sigma_{\mathbf{x}}^{\mathbf{x}}$  is to increase the ratio  $V_r/V_c$ .

When one deals with applied problems using a gas-controlled heat pipe one frequently has to stabilize the temperature of the external condenser surface, for which the temperature-sensitivity coefficient has the form

$$\sigma_{\rm c}^{*} = \left[ \sigma_{\rm v}^{*-1} - \frac{Q_{\rm max} R_{\rm a}^{'}/F_{\rm max} - Q_{\rm min} R_{\rm a}^{'}/F_{\rm min}}{Q_{\rm max} - Q_{\rm min}} \right]^{-1}.$$
 (24)

Analysis shows that the second term in Eq. (24) begins to dominate for large values of  $\sigma_v^*$ .

The general temperature-sensitivity coefficient for the external evaporator surface can be written in the form

$$\sigma_{\rm v}^* = \left[ \sigma_{\rm v}^{*-1} - \frac{R_{\rm e}'}{F_{\rm e}} \right]^{-1}.$$
(25)

In this expression  $\sigma_v^*$  is determined in conjunction with Eq. (23).

Analysis of Eq. (25) shows that an unlimited increase in the temperature-sensitivity coefficient of the vapor leads to a situation where the second term in the expression begins to dominate. Figure 4 shows calculated values of  $\sigma_e^* = f(\sigma_v^*)$  for certain ratios  $R_e^*/F_e$ . From the figure it can be seen that each of the curves represented has two asymptotes. With an increase in  $\sigma_v^*$  the curve draws near to the asymptote  $\sigma_e^* = F_e/R_e$ , and for a decrease in  $\sigma_v^*$  it draws near to the asymptote  $\sigma_e^* = \sigma_v^*$ . Therefore, in order to obtain a high evaporator temperature stabilization, one must increase the heat supply area and decrease the thermal resistance of the evaporator. In analogy with the limit in heat transmission in porous heat pipes, one can introduce a bound on thermal stabilization in gas-controlled heat pipes:

$$\sigma_e^* \rightarrow \frac{F_e}{R'_e} \quad \text{as} \quad \sigma_v^* \rightarrow \infty.$$
 (26)

For an experimental check of the design relationships obtained, we investigated lowtemperature gas-controlled heat pipes using distilled water and ethanol. The experimental results for the temperature-stabilizing parameters were presented in [8, 9]. Good agreement was obtained between the experimental data and the theoretical relationships (16), (22), and (23). The experimental values of the temperature-sensitivity coefficient differed from the theoretical values by 15%.

### NOTATION

L, length; T, temperature; F, area; Q, heat flux; M, molecular weight; Ro, universal gas constant; m, mass; r\*, latent heat of vaporization; V, volume; I, perimeter; R, total thermal resistance; R', reduced thermal resistance;  $\sigma^*$ , temperature-sensitivity coefficient; P, pressure; o, surface-tension coefficient; p, density; µ, dynamic viscosity. Indices: h.p, heat pipe; g, gas; a, active zone of condenser; c, condenser; s, heat source; r, gas reservoir; e, evaporator; o, operating range; cr, critical point; tr, triple point; w, wall; wk, wick; l, liquid; a.z, adiabatic zone; v, vapor; hta, heat-transfer agent.

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EXPERIMENTAL INVESTIGATION OF THE THERMODYNAMIC

CRISIS OF FILM BOILING

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UDC 536.423.1

It is shown on the basis of experimental data that the thermodynamic crisis of film boiling depends on the material at the surface of the cooled solid. A theory substantiating the effect of the thermophysical characteristics of the surface on the crisis temperature in steady-state film boiling is proposed.

Reduction of the cooling time for metal structures washed by low-boiling liquids constitutes a pressing problem involving many cryogenic systems and devices. In cooling objects to operating temperatures under conditions where the vapor temperature near the vapor filmdispersoid boundary is close to the saturation temperature, the total cooling time can be reduced by diminishing the relative share of the wall's heat resource taken off during film boiling, i.e., by switching to intermediate, more intensive types of boiling at a temperature higher than  $T = T_{L_D}$ .

Many investigators have noted on the basis of experimental results that the film boiling crisis, the transition to nucleate boiling, depends on the material at the surface of the cooled solid [1-5]. In particular, it has been found that coating of the solid to be cooled with a thin film of a material possessing a low thermal-conductivity coefficient sometimes leads to a higher temperature of thermodynamic crisis of film boiling. With the exception of [1], the many attempts at explaining this phenomenon were unsuccessful. In our opinion, this is due to a lack of a sufficient amount of experimental data and the contradictory nature of the data on the relative effect on the film boiling crisis of coating the parts to be cooled with various materials. It has been proved [3] that a stationary model cannot be used to explain the effect of coatings (or the effect of the material at the surface). On the other hand, in many cases an increase in the coating thickness (beyond certain values) had a similar effect on the cooling rate of a solid, as in the case of the stationary model. This necessitated new theoretical and experimental investigations.

Figures 1 and 2 show the effect of various coatings and of their thickness on the cooling time of specimens in liquid nitrogen. The cooling is accelerated as a result of passage to efficient types of boiling (in comparison with stable film boiling) at higher mean temperatures of the specimen.

The experimental values of the mean-mass temperature of a solid cooled in liquid nitrogen corresponding to the crisis of stable film boiling are obtained by processing the cooling curves  $T(\tau)$  for the experimental specimens, the dimensions of which are determined (on the basis of theoretical estimates, using the similarity theory and regular conditions) with an allowance for the virtual absence of a temperature gradient along the wall thickness; i.e., Bi  $\ll$  1 and T<sub>w</sub>  $\cong$  T<sub>wo</sub>. The temperature of the experimental specimen at the time of sharp change in the slope of the cooling curve is used as the temperature boundary of the thermodynamic crisis of film boiling (Fig. 3).

The absence of a clearly defined temperature boundary of change under the heat-transfer conditions is a characteristic of the film boiling crisis. This cannot be explained only by the adopted method of experimental data processing; it is connected with the complex effect

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